

# 扬声器单元振动和声辐射的力学分布式参数

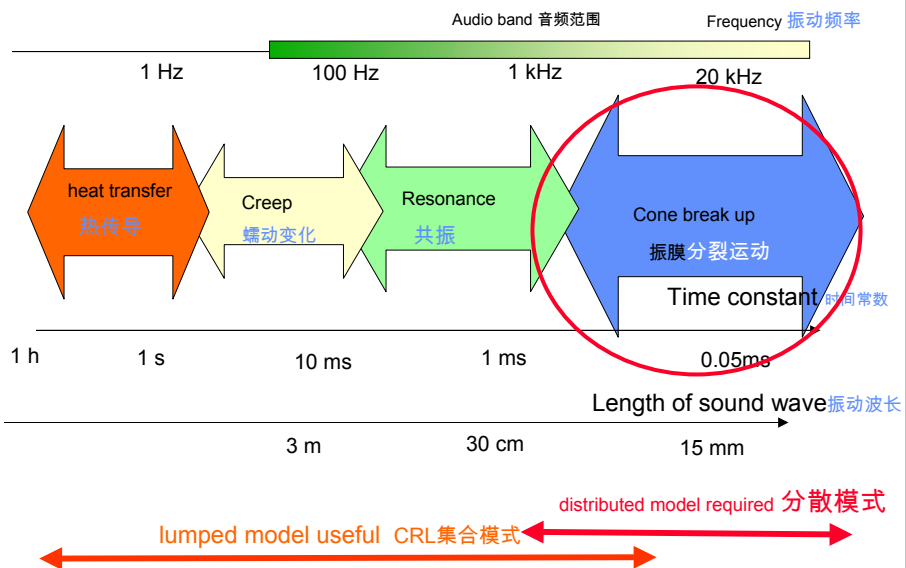
Distributed mechanical parameters describing vibration and sound radiation of loudspeaker drive units

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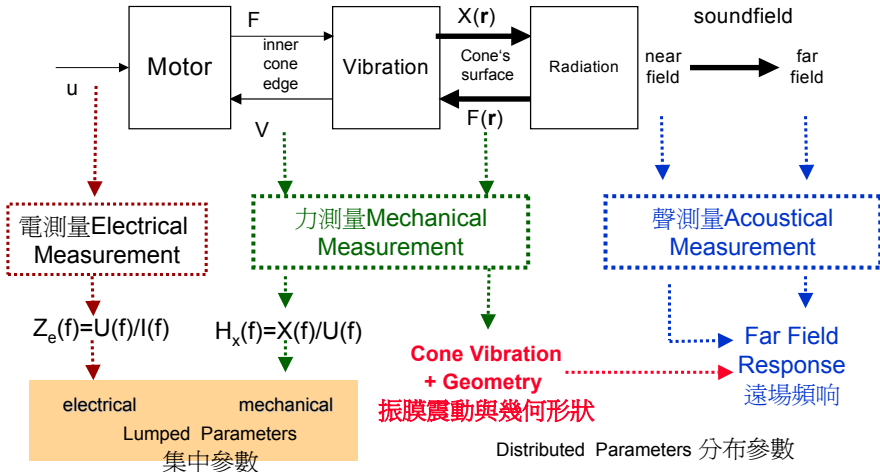
## 扬声器 - 一个动态系统

Loudspeaker - a dynamic system



# 測量為揚聲器偵錯的基礎

Measurements are the basis for loudspeaker diagnostics



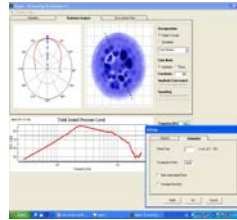
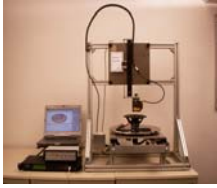
# 振膜掃描技術

Cone Scanning Techniques

Amplitude 振幅	Amplitude+ phase 振幅+相位	Amplitude + phase + geometry 振幅 相位 幾何形狀
<p><b>Olson, 1950</b></p>	<p><b>Doppler Interferometry</b> 杜普勒干涉激光掃描 (Polytech, 1995)</p> <p>Velocity distribution on the cone 錐體速率分布</p>	<p><b>Triangulation Laser Scanner</b> 三角測量激光掃描儀 (Klippel, 2007)</p> <p>Geometry 幾何形狀 Displacement 位移</p>
<p><b>Frankort 1978</b></p> <p>Intensity 強度</p>		

# 扬声器设计的新工具

## New Tools for Loudspeaker Design



### 扫描设备 Scanner Hardware

- 专为分析扬声器开发  
Dedicated to loudspeakers
- 经济的价格 Price effective
- 扫描几何形状 Scanning geometry
- 更多其它的应用 Many other applications

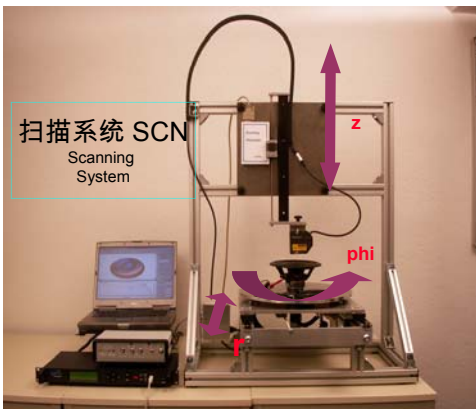
### 软件分析 Analyzer Software

- 振膜振动可视化  
Visualization of cone vibration
- 输出声压的预测 Prediction of sound pressure output
- 指向性 Directivity
- 可分解振动模式以利分析  
Decomposition

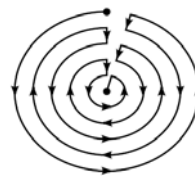


# 自动化扫描过程

## Automatic Scanning Process



机械扫描系统包括一个转动和二线性致动器  
Mechanical scanning system with one rotational ( $\phi$ ) and two linear actuators ( $r, z$ )



扫描过程从外缘开始逐渐向里推进  
The scanning starts at the outside rim and proceeds inwards



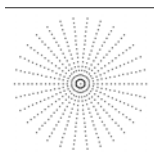
# 扫描模式 Scanning Modes

剖面扫描 Profile Scan



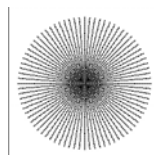
适用于 Good for  
• 只有轴对称辐射  
Radiation of  
axial-symmetrical  
Geometries only

探索扫描 Explore Scan



适用于 Good for  
• 所有振膜辐射  
Radiation all cones  
• 摇摆模式 Rocking modes

详细扫描 Detailed Scan



适用于 Good for  
• 不规则振动 Irregularities

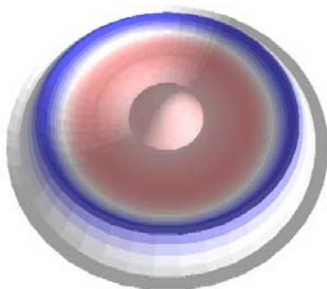
扫描时间 Scanning Time



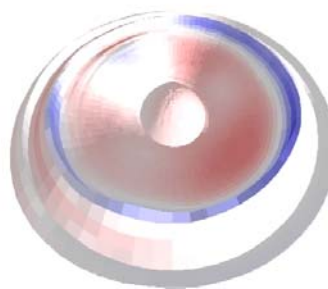
## 剖面扫描是很有用的！

A Profile Scan is already useful !

剖面扫描 Profile Scan



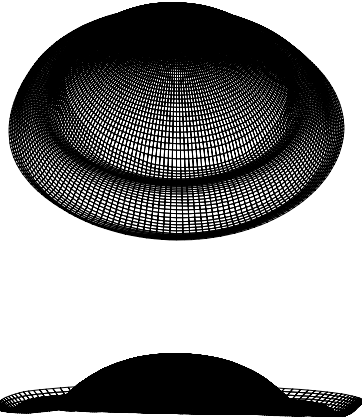
详细扫描 Detailed Scan



# 测量几何形状

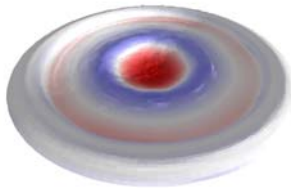
## Measurement of Geometry

- 高精度 High Precision  
 $< 10 \mu\text{m}$  for  $0 < z < 300 \text{ mm}$   
 $< 2.5 \mu\text{m}$  for  $-5 \text{ mm} < z < 5 \text{ mm}$
- 双相关测量 Dual Measurement with correlation
- 自动检测光学误差 Automatic detection of optical errors
- 以常见文本或DXF格式输出 Export in common formats (如 such as \*.txt, \*.dxf)

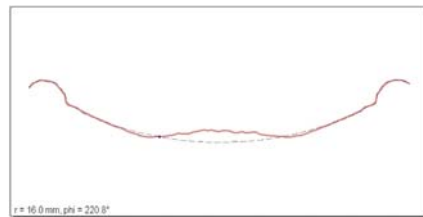


# 振动数据可视化

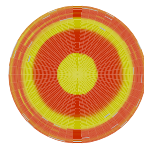
## Visualization of Vibration Data



三维动画 3D Animation



横断面削减 Cross-sectional Cut



相位分布 Phase Distribution



振幅分布 Amplitude Distribution



# 軟體分析

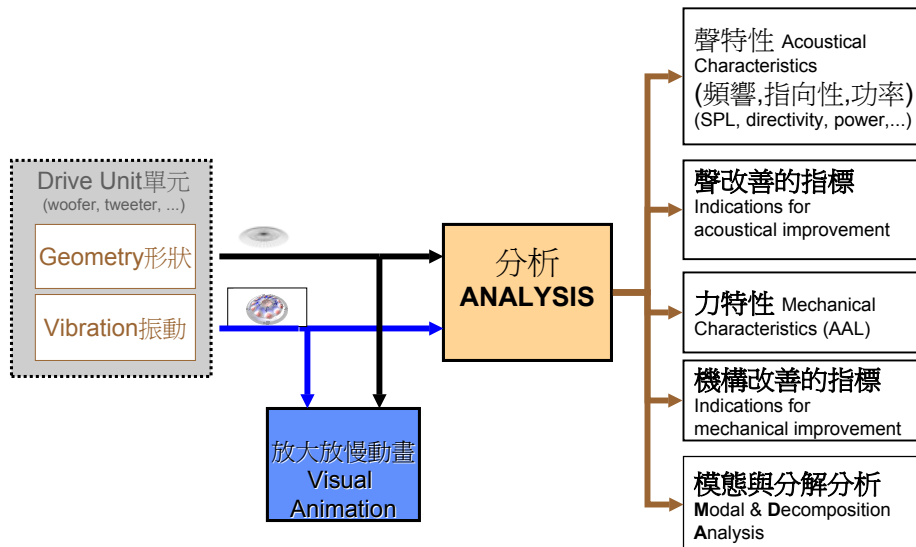
Analysis Software

## 任務Tasks:

- 偵測及減少錯誤 Detect and suppress errors
- 振動可视化 Animate vibration
- 让分析更容易 Make interpretation simpler
- 增強对設計重要的資訊 Enhance information which are important for design
- 預測輸出音壓 Predict sound pressure output

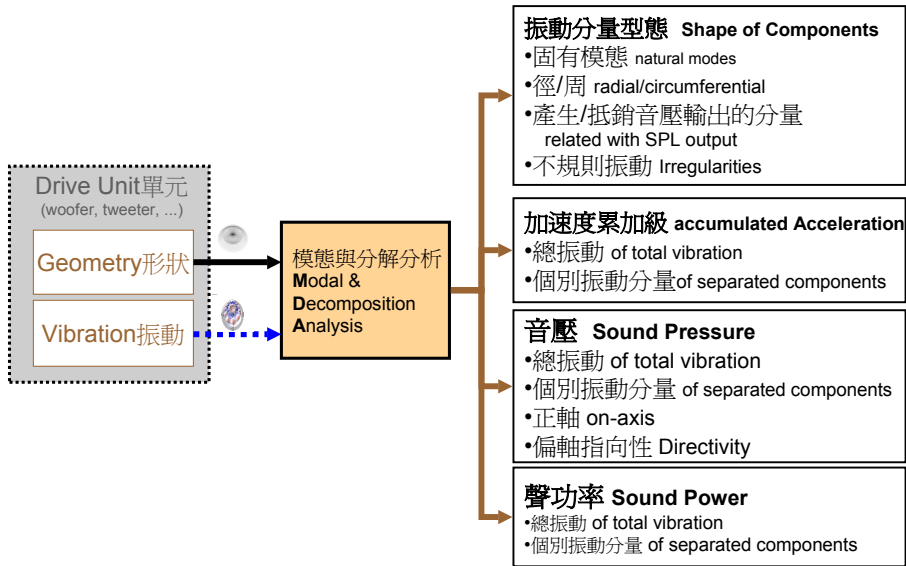
## 動輻射分析需要複數振動資料與幾何形狀

Vibration and Radiation Diagnostics needs complex vibration data + cone geometry



# 根據掃描資料作振動及輻射診斷

## Vibration and Radiation Diagnostics based on Scanning Data



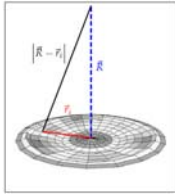
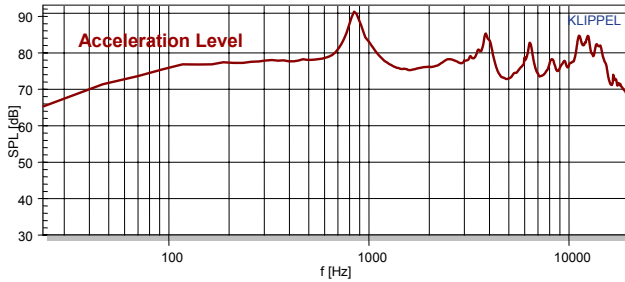
# 檢查振膜的振動

## Checking Cone Vibration

- 有足夠的振動振幅了嗎？  
Do we have enough vibrational amplitude ?
- 在振膜的哪一個部分最先出現分裂模式？  
On which cone part first break-up modes occur ?
- 分裂振動模態是否逐漸取代活塞運動模式？  
Does the break-up modes gradually replace the piston mode ?
- 有膜振動模態或彎曲振動模態嗎？  
Do we have membrane or bending modes ?

# 累積加速度級

## Accumulated Acceleration Level



$$a_a(j\omega, \vec{r}_a) = \frac{\omega^2 \rho_0}{2\pi} \int_{S_c} \frac{X(j\omega, \vec{r}_c)}{|r_a - r_c|} dS_c$$

$$AAL(\omega, \vec{r}_a) = 20 \log \left( \frac{a_a(j\omega, \vec{r}_a)}{p_o} \right) \text{ dB}$$

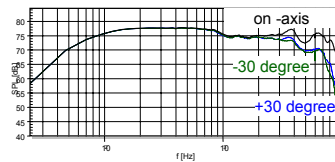
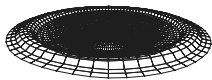
Weighted Sum of the acceleration amplitude

加速度幅度的加權積分

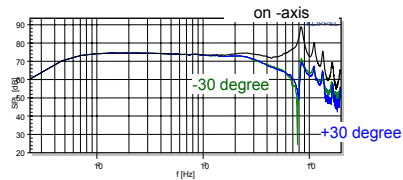
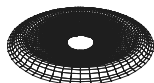
# 要平坦靈敏度響應曲線? 正軸? 偏軸?

## Smooth SPL Response ?

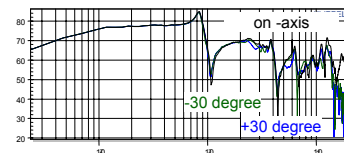
Woofer A with paper cone



Woofer B with magnesium cone



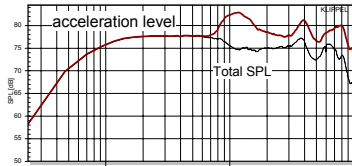
Woofer C with flat radiator



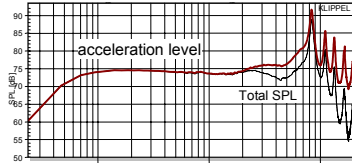


# 錐盆的振動足夠嗎?

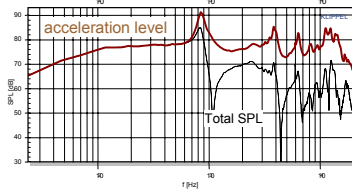
## Sufficient Cone Vibration ?



紙盆低音 Woofer A with paper cone :  
 → 低品質因數共振的紙盆  
 low Q factor of cone resonances



鎂鋁盆低音 Woofer B with magnesium cone:  
 → 通常高頻有高品質因數共振的峰值  
 natural modes cause high peaks in SPL



平板低音 Woofer C with flat radiator  
 → 累積加速度級不易見低谷  
 dips are not visible in AAL  
 → 累積加速度級在 800 Hz 時有一個峰值  
 AAL cause peak at 0.8 kHz



# 怎樣做模態分析?

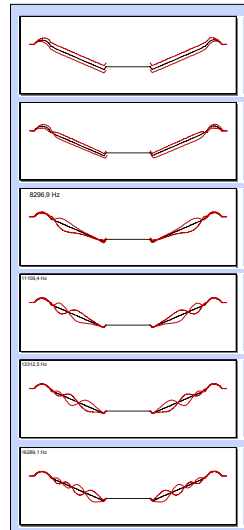
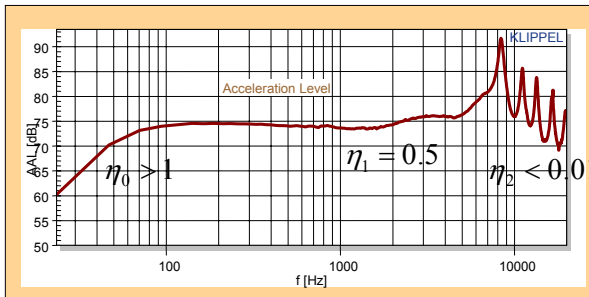
## How to perform modal analysis ?

在累積加速度中找極大值

Search for maxima in accumulated acceleration !

$$a_a(j\omega) = \frac{\rho_0}{2\pi} \sum_{i=0}^{\infty} \frac{\omega^2}{1 + \eta_i j\omega/\omega_i - (\omega/\omega_i)^2} \int_{S_c} |\psi_i(r_c)| |r_a - r_c| dS_c$$

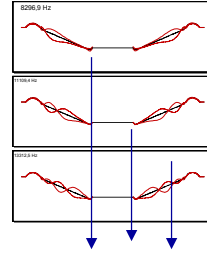
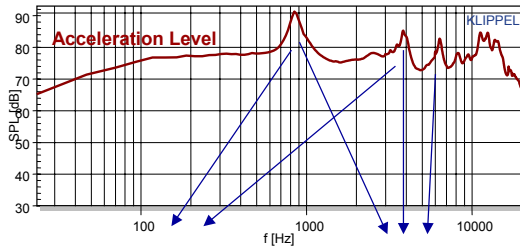
positive value



# 如何定立輻射體規格?

How to Specify the Radiator ?

锥体, 振膜和懸邊 Cone, Diaphragm and Surround



Modal loss factor  $\eta_i$  of each mode  $i^{\text{th}}$ -mode with  $i=1,2,\dots$

材料的損耗因數  
Loss factor of the material

Natural frequency  $f_i$  of the  $i^{\text{th}}$ -mode with  $i=1,2,\dots$

材料的Young's系數  
Young's E Modulus of the material

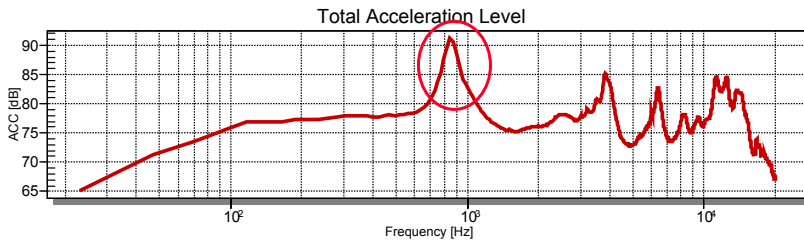
Natural Function  $\Psi_i(r_0)$  of each mode  $i^{\text{th}}$ -mode with  $i=1,2,\dots$

輻射體的结构(外形, 厚度)  
Geometry of the Radiator  
(shape, thickness, ..)

# 材質有足夠的阻尼嗎?

Sufficient Damping of the Material ?

Woofer C with flat radiator



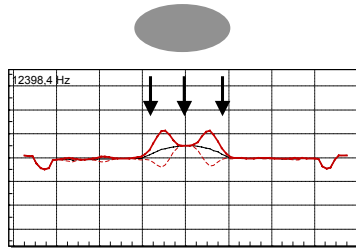
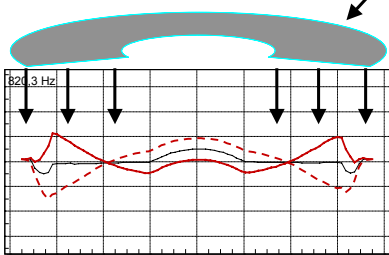
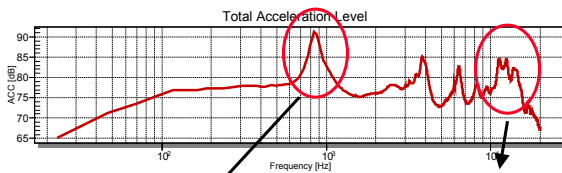
在累積加速度級中找共振衰減3dB頻寬  
Read 3dB bandwidth in AAL

$$\eta_i = \frac{f_{i+} - f_{i-}}{f_i} = \frac{80}{840} \approx 0.1$$

→ Increase loss factor of material  
→ 增加材料的阻尼

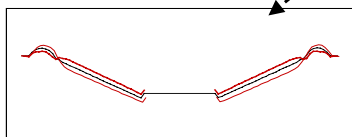
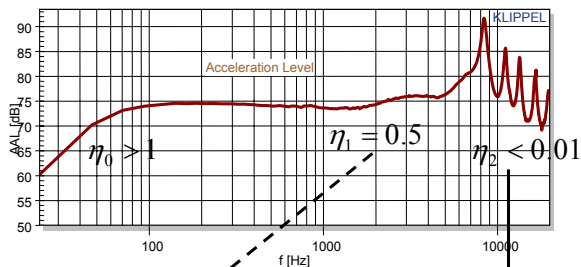
# 在何處增加阻尼?

Where to apply additional damping?  
woofer C with flat radiator

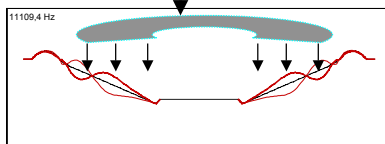


# 在何處增加阻尼?

Where to apply additional damping?  
Woofer B Magnesium cone



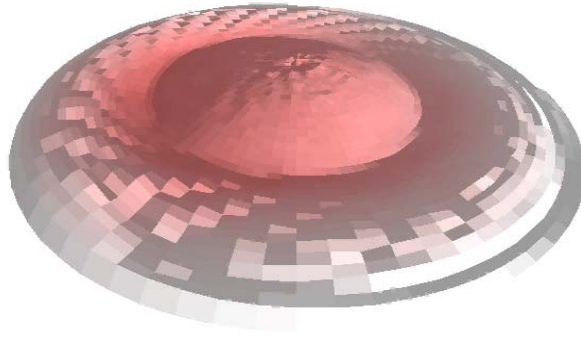
Rubber surround has sufficient losses  
懸邊有足夠損耗使中頻平坦



Cone requires damping  
膜振動需加強阻尼

# 微型扬声器

Microspeaker 13 mm

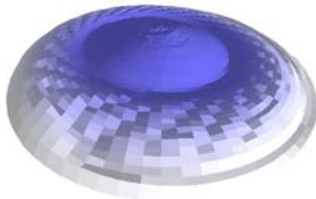


## 辐射分解为周分量及圆分量

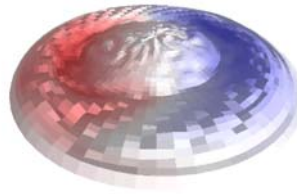
Decomposition into radial and circular components

$$\bar{x}_{total} = \bar{x}_{rad} + \bar{x}_{circ}$$

At 580 Hz



Radial vibration mode  
周振动模式



Circular vibration mode  
圆振动模式

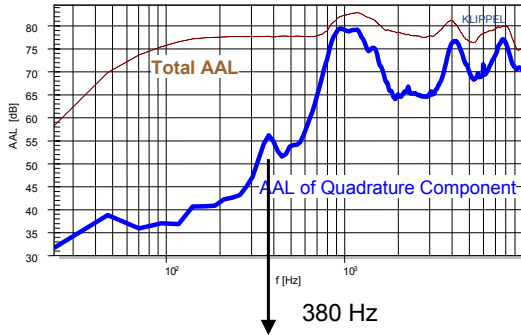
↓  
causes Rub & Buzz  
促使異音產生



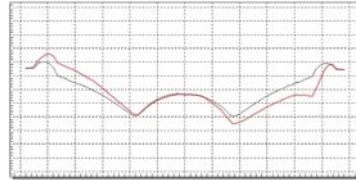
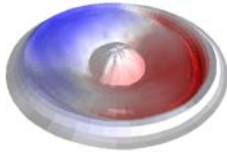
# 如何找出搖擺模態

How to find rocking modes ?

Woofer A with paper cone

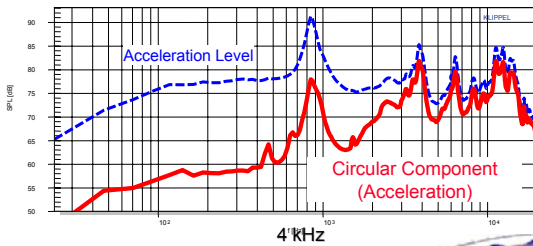


Search for maximum in quadrature component in AAL at low frequencies  
在累積加速度級正交分量中找低頻極大值

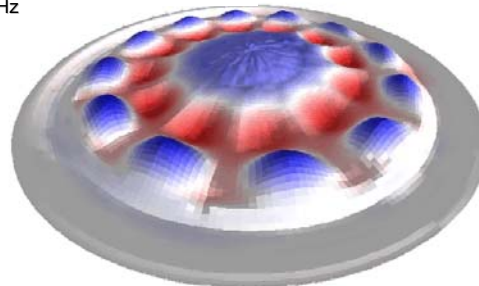


# 主要的環狀模態

Dominant Circumferential Modes ?



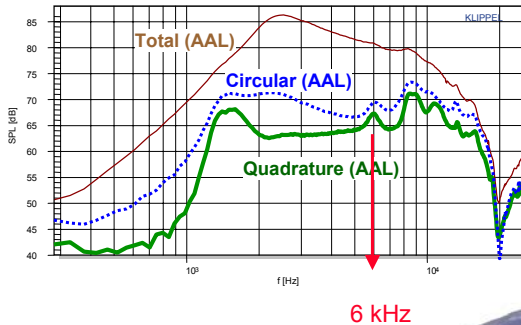
Woofer C with flat radiator



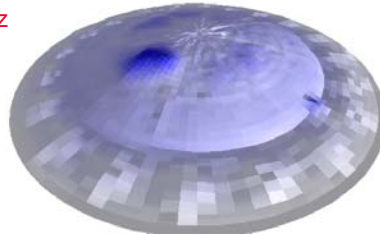
# 如何找出不規則的振動？

## How to find irregular Vibrations ?

Aluminum diaphragm of a horn compression driver



Search for maximum in quadrature or circular component of AAL  
在AAL累積加速度級的正交分量或圓分量中找極大值



# 檢查輻射問題

## Checking radiation problems

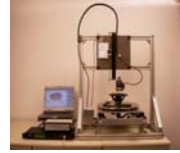
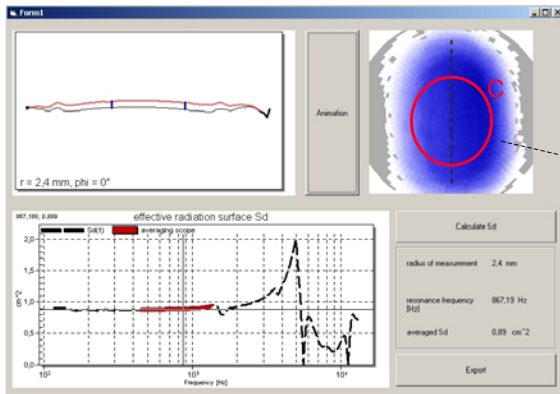
- 有明顯的抵銷效應嗎？  
Do we have a strong cancellation effect?
- 抵銷效應是否影響偏軸響應？  
Does the cancellation affect out-off axis points ?
- 振膜的哪一個部分輻射聲音？  
Which cone part radiates sound ?
- 輻射面積是不是在逐漸減小？  
Does the size of radiating area decreases gradually ?

# 雷射掃描技術如何測得有效振動面積

(精準全自動的方法)

## How to Measure Radiation Area $S_d$ ?

Laser Scanner Technique (precise, robust)



Integration of  $x$  on curve  $C$

$$\Delta x = \frac{\int_C x(r) dr}{C}$$

$$S_d = \frac{\Delta V}{\Delta x} = \frac{\int_S x(r) dS}{\Delta x}$$

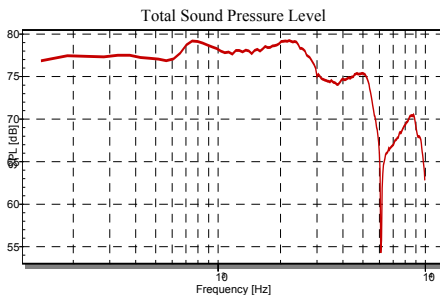
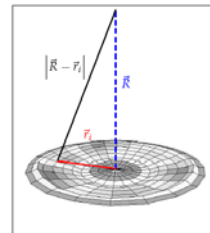
Under klippel development

# 声压的预测

## Prediction of Sound Pressure

Rayleigh积分公式 Rayleigh Integral Equation

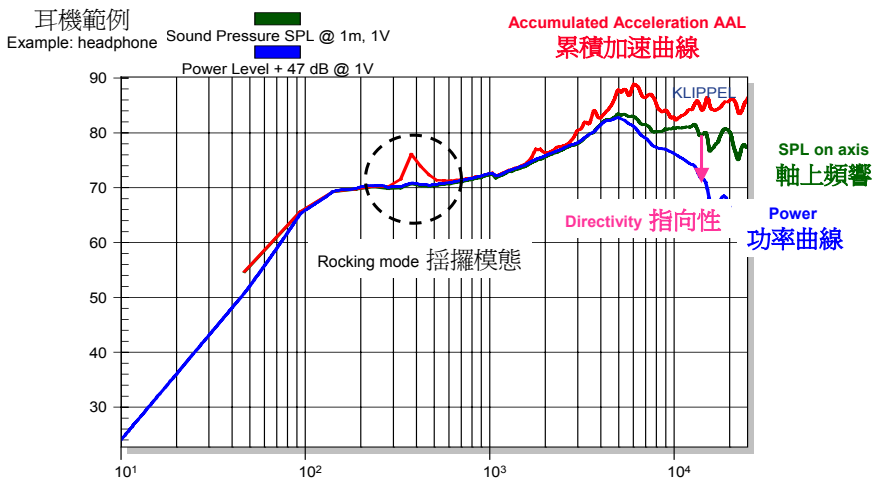
$$p(\vec{R}, \omega) = -\frac{\omega^2 \rho_0}{2\pi} \int_S \frac{e^{-jk_0 |\vec{R} - \vec{r}_i|}}{|\vec{R} - \vec{r}_i|} x_n(\vec{r}_i) dS$$



- 单体位于无限障板中
- driver in infinite baffle
- 对大部份的角度有足够好的近似
- good approximation for most angles
- 计算时间短 short calculation time

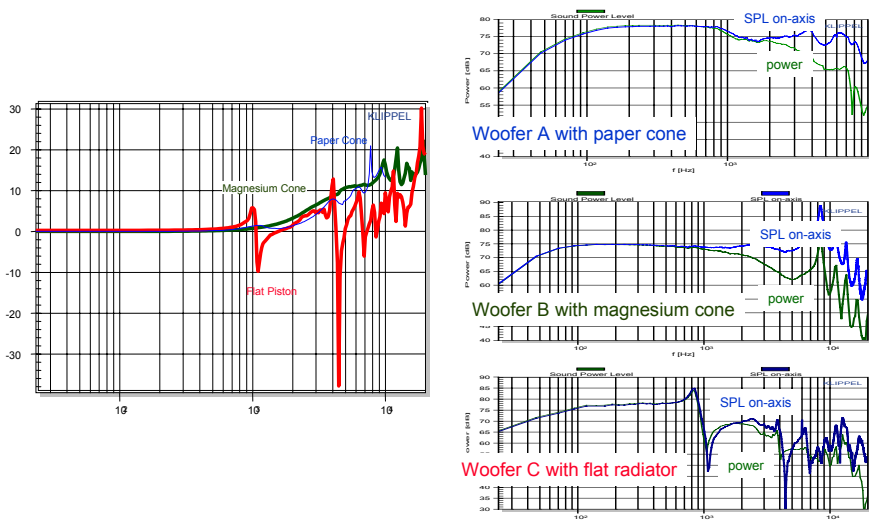
# 重要結論

## Most important Results



# 想要的指向性？

## Desired Directivity ?

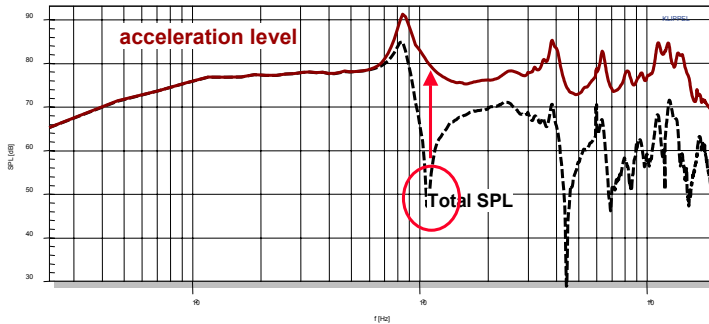




# 為何產生頻響上的低谷?

## What causes the dips in SPL ? Woofer C with flat radiator

→ Compare Accumulated Acceleration (AAL) with sound pressure (SPL)  
→ 比對累積加速度級與聲壓級

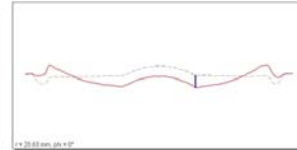
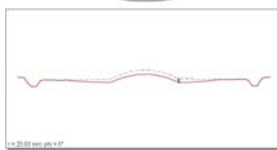
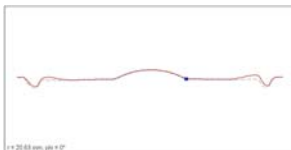
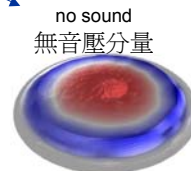
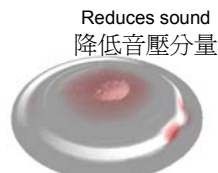
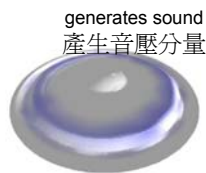


There is enough vibration on the cone !! → Radiation Problem  
如果有足夠加速度, 但沒聲壓 -> 代表輻射問題



# 音壓相關的分量分解 Sound Pressure related Decomposition

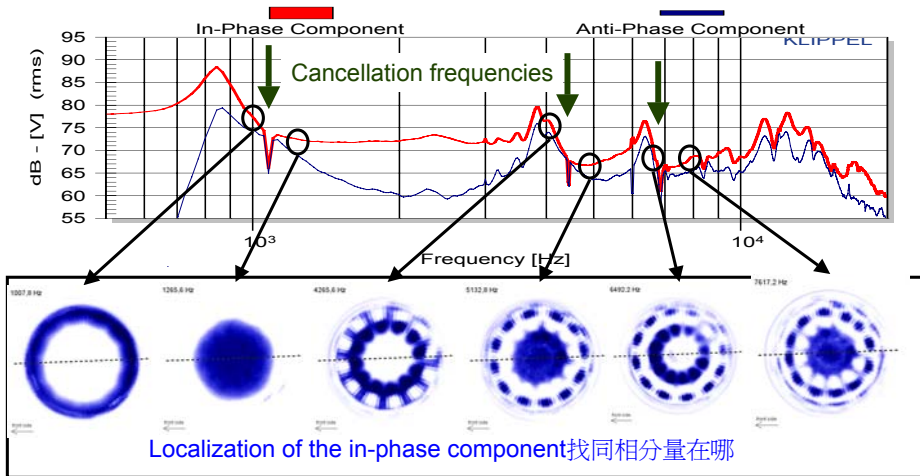
$$\bar{x}_{total} = \bar{x}_{in} + \bar{x}_{anti} + \bar{x}_{quadrature}$$



# 振膜哪部分輻射出聲音?

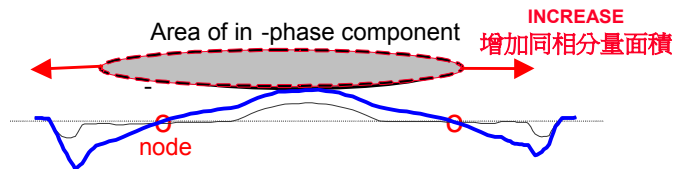
Where is the sound radiated ?

Woofer C with flat radiator



# 如何解決聲抵消問題?

How to Fix Acoustical Cancellation problems ?



目標 Target:

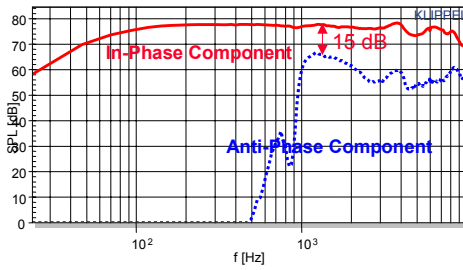
- 使同相分量主導 Make in-Phase component dominant
- 抑制反向分量 Suppress anti-phase component

步驟 Steps:

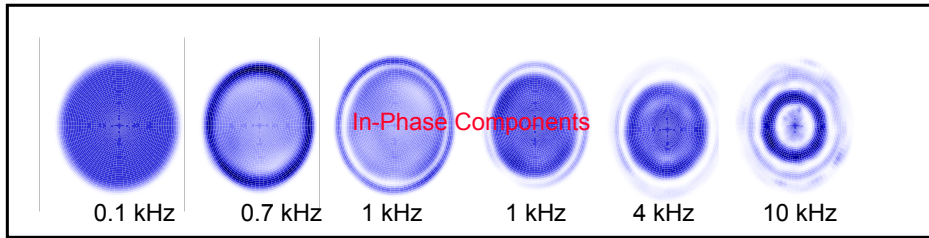
1. 找同相分量位置 find location of in-phase component
2. 用有限元分析模擬振動模式 use FEA to simulate behavior
3. 在這部分加強抗彎曲強度(變厚, 加弧度, 加補強筋) increase bending stiffness at this area (thickness, curvature, ribs)

# 聲音向何處輻射? Where is the sound radiated ?

Woofer A: Paper Cone



- 同相分量主導 In-phase component is dominant
- 無聲音抵銷 No acoustical cancellation
- 同相分量保持在振膜中間 In-phase component stays in the centre
- 輻射面積隨頻率縮小 radiation area shrinks with frequency



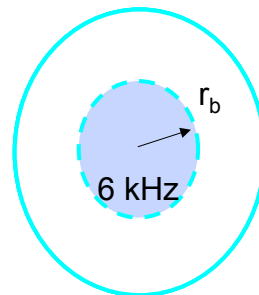
扬声器单元振动和声辐射的力学分布式参数 Distributed mechanical parameters 37

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## 提示:减少纸盆有效面积

TIP: Reduction of effective cone area

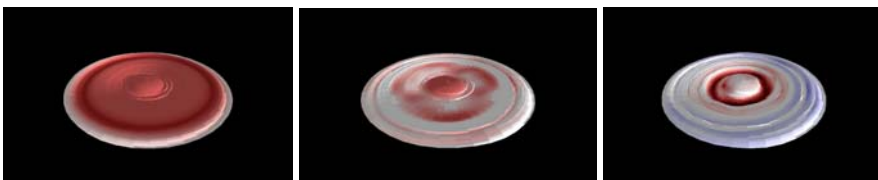
- 分裂始于外部 Breakup starts outside
- 外环面积不能辐射明显的音压 Outer ring area does not radiate significant sound
- 内部应辐射音压 (同相分量) Inner part should radiate sound (in-phase component)



500 Hz

3 kHz

7 kHz



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# 結論

## Conclusion

- 位移感測器 + 掃描器 + 信號處理  
Displacement sensors + scanner + signal processing  
→ 成本經濟的揚聲器振動模態測量  
cost effective solution for loudspeaker vibrometry
- 幾何形狀 + 振動資料是分析的基礎  
Geometry + Vibration data is basis for analysis
- 振動和輻射之間的相互影響是很重要的  
Interaction between vibration + radiation are important
- 新的分量分解技術 → 簡化解讀  
New decomposition techniques → simplifies interpretation

